

# Seminar: Medical Image Processing

A robust approach for automatic detection and segmentation of cracks in underground pipeline images

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# Roadmap

**1** Introduction

**2** Morphology

**3** Linear filters

**4** Detection

**5** Evaluation

**6** Summary

## Discussed papers

- Shivprakash Iyer and Sunil K. Sinha: A robust approach for automatic detection and segmentation of cracks in underground pipeline images. *Image and Vision Computing*, 23:921-933, 2005.

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- Frederic Zana and Jean-Claude Klein: Segmentation of vessel-like patterns using mathematical morphology and curvature evaluation. *IEEE Transactions on Image Processing*, 10(7):1010-1019, July 2001.

# The situation

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Large underground sewer networks need continuous checks.

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Reliable *automated defect detection* and classification system desirable to compensate these problems

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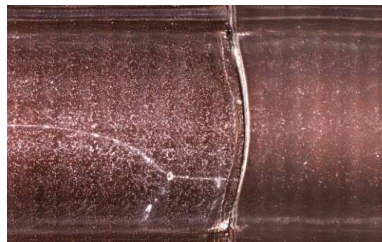
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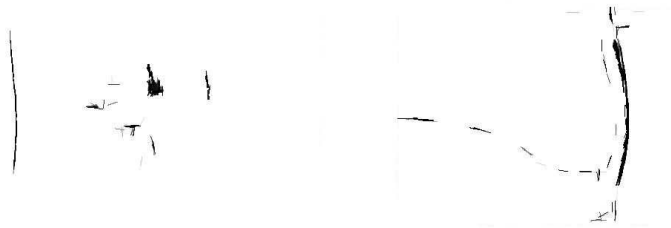
# What are cracks?

- Large linear portions
- Branch like a tree
- Intensity distribution of a crack feature cross-section looks like a specific gaussian curve
- More or less constant width
- Retinal vessels: similar features  $\Rightarrow$  similar method works to segment vessels

# Examples (cracks and retinal vessels)



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# Processing pipeline structure

- Usage of mathematical morphology (MM) and linear filters (LF)

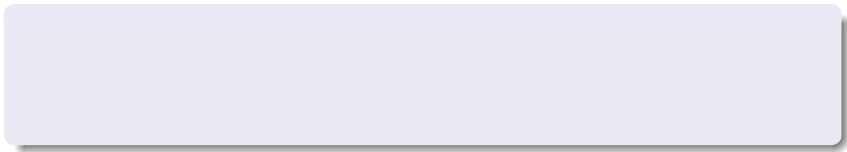


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- 1** Preprocessing (contrast enhancement)
- 2** Enhancement of cracks (MM and LF)
- 3** Segmentation of cracks (MM alternating filters)

1 Introduction

**2 Morphology**

- What is mathematical morphology?
- Morphology operations
- Specific parameters for crack detection

3 Linear filters

4 Detection

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- Extract features based on a priori knowledge about object geometry
- Set-theoretic method providing a quantitative description of geometric structures
- Based on expanding and shrinking operations with regard to a given structuring element (knowledge about object)
- Originally for B/W images, extended for gray images (interesting case here)

# Definitions

*Images* are defined as a function mapping from points to intensity values (here: grayscale,  $I_{min} = 0$  and  $I_{max} = 255$ ):

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Binary *structuring elements* (SE) are defined as a function:

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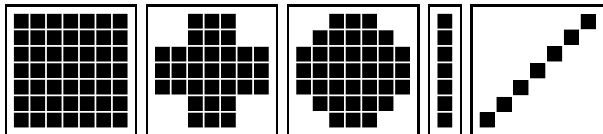
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# Important notation specialties for crack detection

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- Foreground: white
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*Some operations change meaning:*

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- Shrinking

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- Expanding

# Dilation

$$\delta_B^e(F)(P_0) = \max_{P \in P_0 \cup e \cdot B(P_0)} (F(P))$$

- Basic *expanding* operation.

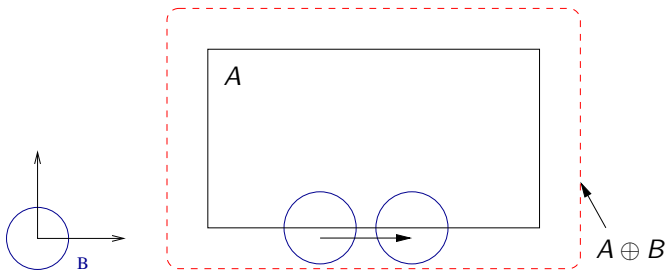
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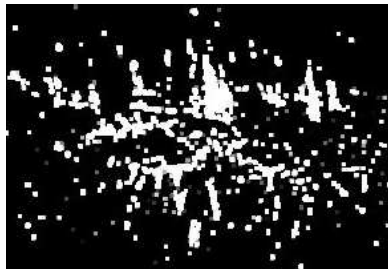
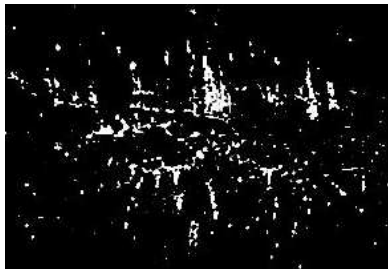


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- Basic *shrinking* operation.

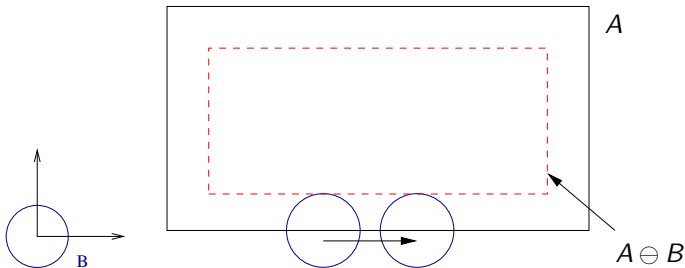
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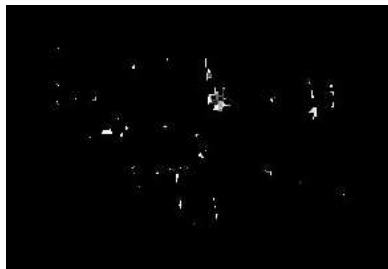
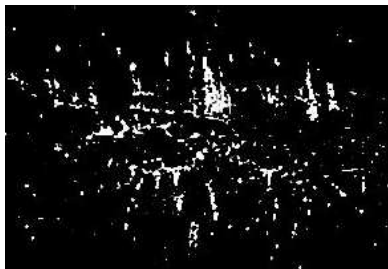


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$$\gamma_B^e(F) = \delta_B^e(\varepsilon_B^e(F))$$

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*(basic opening by  $3 \times 3$  square SE: original image)*

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- Example: edge detection using top-hat filter



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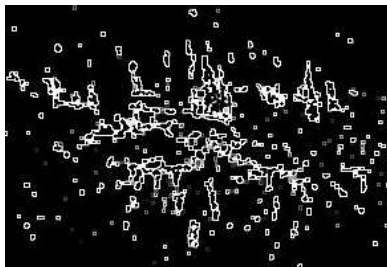
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*(edge detection by top-hat: top-hat with original image)*

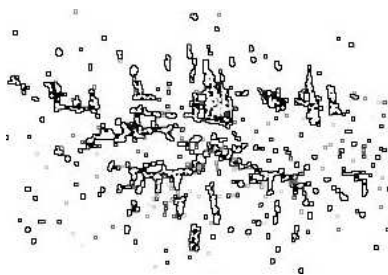


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- Instead of one image and a SE now two images are used
- *Marker* image is source image, *mask* image is max. or min. image (depending on operation)
- Geodesic: Extracts connected components based on distance
- Can be used with different morphological operations

# Geodesic reconstruction by erosion (geodesic closing)

$$\Phi(F, G) = \varepsilon_G^{(n)}(F) = \max \left( G, \varepsilon_G^{(n-1)}(\varepsilon_B(F)) \right)$$

- $B$  Isotropic structuring element
- $F$  Image (Marker)
- $G$  Image (Mask)
- $\varepsilon$  Erosion
- $\varepsilon_{B,G}^{(0)}(F) = F$
- $n$  number of iterations until stability has been reached
- $(\varepsilon_{B,G}^{(n)}(F) = \varepsilon_{B,G}^{(n+1)}(F) \text{ holds})$

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## 1 Erode marker image



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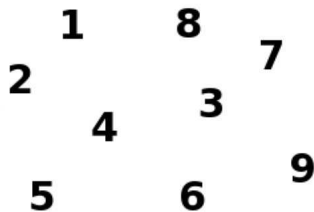
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- 2 Take maximum of eroded image and mask image
- 3 If image has been changed in this iteration goto 1

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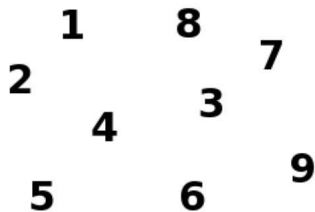


*(segment 1 and 4: original image)*

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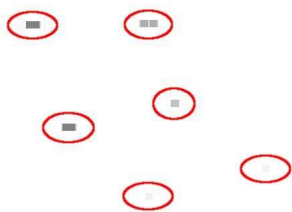
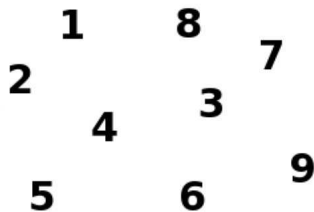


*(segment 1 and 4: dilation by linear SE, length = 45 pixel, vertical)*

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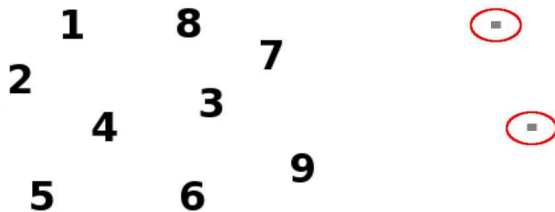


(segment 1 and 4: marked dilation result)

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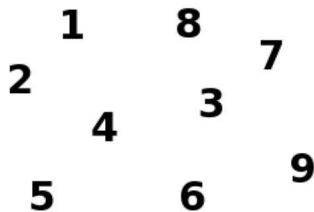


*(segment 1 and 4: dilation by linear SE, length = 7, horizontal)*

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- $B$  Isotropic structuring element
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- $G$  Image (Mask)
- $\varepsilon$  Erosion
- $\varepsilon_{B,G}^{(0)}(F) = F$
- $n$  number of iterations until stability has been reached ( $\varepsilon_{B,G}^{(n)}(F) = \varepsilon_{B,G}^{(n+1)}(F)$  holds)

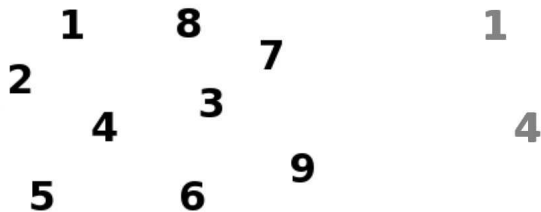


*(segment 1 and 4: un-marked dilation result)*

# Geodesic reconstruction by erosion (geodesic closing)

$$\Phi(F, G) = \varepsilon_G^{(n)}(F) = \max\left(G, \varepsilon_G^{(n-1)}(\varepsilon_B(F))\right)$$

- $B$  Isotropic structuring element
- $F$  Image (Marker)
- $G$  Image (Mask)
- $\varepsilon$  Erosion
- $\varepsilon_{B,G}^{(0)}(F) = F$
- $n$  number of iterations until stability has been reached ( $\varepsilon_{B,G}^{(n)}(F) = \varepsilon_{B,G}^{(n+1)}(F)$  holds)



*(segment 1 and 4: geodesic reconstruction with original as mask)*



# Geodesic reconstruction by dilation (geodesic opening)

$$\Gamma(F, G) = \delta_G^{(n)}(F) = \min \left( G, \delta_G^{(n-1)}(\delta_B(F)) \right)$$

$B$	Isotropic structuring element
$F$	Image (Marker)
$G$	Image (Mask)
$\delta$	Dilation
	$\delta_{B,G}^{(0)}(F) = F$
$n$	number of iterations until stability has been reached
	$(\delta_{B,G}^{(n)}(F) = \delta_{B,G}^{(n+1)}(F))$ holds

- 1 Dilate marker image
- 2 Take minimum of dilated image and mask image
- 3 If image has been changed in this iteration goto 1

# Structuring elements

- Based on observation of cracks specific SEs are chosen

# Structuring elements

- Based on observation of cracks specific SEs are chosen
- Linear SE

# Structuring elements

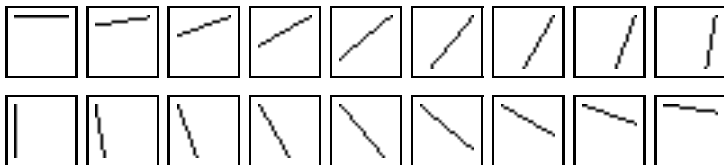
- Based on observation of cracks specific SEs are chosen
- Linear SE
- SE length: 12 pixel

# Structuring elements

- Based on observation of cracks specific SEs are chosen
- Linear SE
- SE length: 12 pixel
- Degree of rotation: every  $10^\circ$  from  $0^\circ$  to  $180^\circ$

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- Based on observation of cracks specific SEs are chosen
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# Structuring elements

- Based on observation of cracks specific SEs are chosen
- Linear SE
- SE length: 12 pixel
- Degree of rotation: every  $10^\circ$  from  $0^\circ$  to  $180^\circ$



- Filters have been chosen for dark features

1 Introduction

2 Morphology

**3 Linear filters**

- What are linear filters?
- Filters used for crack detection

4 Detection

5 Evaluation

6 Summary



# Linear filters

- Pictures of zebras and dalmatians both have black and white pixels

# Linear filters

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# Linear filters

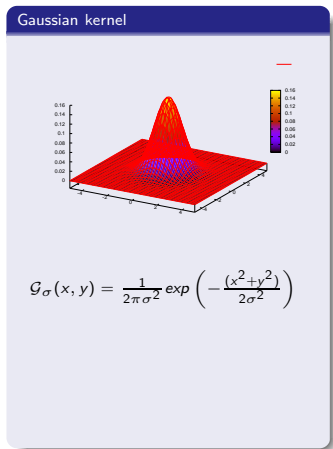
- Pictures of zebras and dalmatians both have black and white pixels
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# Linear filters

- Pictures of zebras and dalmatians both have black and white pixels
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- Difference in order and characteristic appearance of groups
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- Each pixel is set to a weighted sum of its and its neighbours' values (convolution)
- Weights defined as matrix (kernel)
- Here: edge detection

# Gaussian

- Smoothing an image

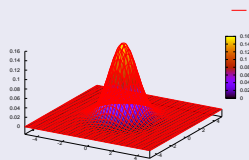




# Gaussian

- Smoothing an image
- Discrete Gaussian kernel from Gaussian function

Gaussian kernel



$$G_{\sigma}(x, y) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{(x^2+y^2)}{2\sigma^2}\right)$$

$$G_1 = \begin{bmatrix} \frac{1}{16} & \frac{2}{16} & \frac{1}{16} \\ \frac{2}{16} & \frac{1}{16} & \frac{1}{16} \\ \frac{1}{16} & \frac{1}{16} & \frac{1}{16} \end{bmatrix}$$

# Gaussian

- Smoothing an image
- Discrete Gaussian kernel from Gaussian function

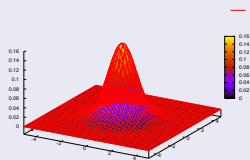


(a) Original



(b) Gaussian

## Gaussian kernel



$$G_{\sigma}(x, y) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{(x^2+y^2)}{2\sigma^2}\right)$$

$$G_1 = \begin{bmatrix} \frac{1}{16} & \frac{2}{16} & \frac{1}{16} \\ \frac{2}{16} & \frac{4}{16} & \frac{2}{16} \\ \frac{1}{16} & \frac{2}{16} & \frac{1}{16} \end{bmatrix}$$

# Laplacian of Gaussian

- Classic method for edge detection

Laplacian of Gaussian kernel



# Laplacian of Gaussian

- Classic method for edge detection

- Laplacian operator:

$$(\nabla^2 f)(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

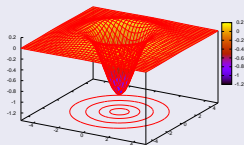
Laplacian of Gaussian kernel

# Laplacian of Gaussian

- Classic method for edge detection
- Laplacian operator:  

$$(\nabla^2 f)(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$
- Natural to smooth before applying laplacian  $\Rightarrow$  Gaussian as function

Laplacian of Gaussian kernel



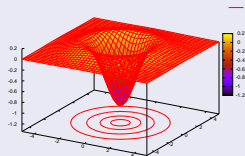
$$\mathcal{L}_\sigma = \frac{(x^2 + y^2 - 2\sigma^2)}{\sigma^4} \exp\left(-\frac{(x^2 + y^2)}{(2\sigma^2)}\right)$$

# Laplacian of Gaussian

- Classic method for edge detection
- Laplacian operator:  

$$(\nabla^2 f)(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$
- Natural to smooth before applying laplacian  $\Rightarrow$  Gaussian as function
- $LoG_{\sigma}^w(F) = F \circ L_{\sigma}^w$   
 (F convolved with L)

Laplacian of Gaussian kernel



$$\mathcal{L}_{\sigma} = \frac{(x^2 + y^2 - 2\sigma^2)}{\sigma^4} \exp\left(-\frac{(x^2 + y^2)}{(2\sigma^2)}\right)$$

$$L_1^5 = \begin{bmatrix} -1 & -3 & -3 & -3 & -1 \\ -3 & 0 & 6 & 0 & -3 \\ -3 & 6 & 21 & 6 & -3 \\ -3 & 0 & 6 & 0 & -3 \\ -1 & -3 & -3 & -3 & -1 \end{bmatrix}$$

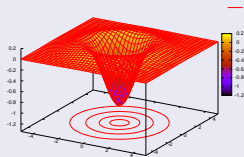
# Laplacian of Gaussian

- Classic method for edge detection
- Laplacian operator:  

$$(\nabla^2 f)(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$
- Natural to smooth before applying laplacian  $\Rightarrow$  Gaussian as function
- $LoG_{\sigma}^w(F) = F \circ L_{\sigma}^w$   
 (F convolved with L)



Laplacian of Gaussian kernel



$$\mathcal{L}_{\sigma} = \frac{(x^2 + y^2 - 2\sigma^2)}{\sigma^4} \exp\left(-\frac{(x^2 + y^2)}{(2\sigma^2)}\right)$$

$$L_1^5 = \begin{bmatrix} -1 & -3 & -3 & -3 & -1 \\ -3 & 0 & 6 & 0 & -3 \\ -3 & 6 & 21 & 6 & -3 \\ -3 & 0 & 6 & 0 & -3 \\ -1 & -3 & -3 & -3 & -1 \end{bmatrix}$$

- 1 Introduction
- 2 Morphology
- 3 Linear filters
- 4 Detection**
  - Detection procedure
- 5 Evaluation
- 6 Summary



# Processing pipeline structure

- Usage of mathematical morphology (MM) and linear filters (LF)
- Results in binary crack map
- Basic 3-step processing pipeline

- 1** Preprocessing (contrast enhancement)
- 2** Enhancement of cracks (MM and LF)
- 3** Segmentation of cracks (MM alternating filters)

# Preprocessing

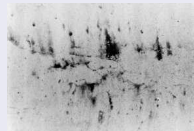
- Goal: Enhance contrast between cracks and background

## Preprocessing pipeline

# Preprocessing

- Goal: Enhance contrast between cracks and background
- 0** Original grayscale image

## Preprocessing pipeline



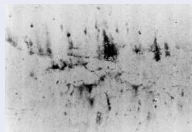
# Preprocessing

- Goal: Enhance contrast between cracks and background

**0** Original grayscale image

**1** Median ( $15 \times 15$ )

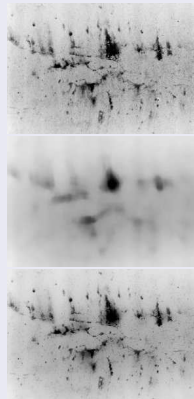
## Preprocessing pipeline



# Preprocessing

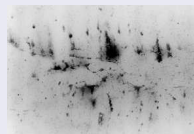
- Goal: Enhance contrast between cracks and background
- 0 Original grayscale image
  - 1 Median ( $15 \times 15$ )
  - 2 Compare foreground (original) and background (median) image, take minimum

## Preprocessing pipeline



# Crack enhancement

## Enhancement pipeline

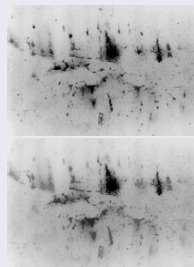


# Crack enhancement

## 1 Closing by Reconstruction

$$F_{CI} = \Phi(\min_{i=1, \dots, 18} \{\phi_{B_i}(F_0)\})$$

### Enhancement pipeline

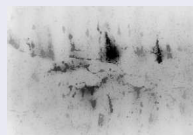


# Crack enhancement

## 1 Closing by Reconstruction

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### Enhancement pipeline





# Crack enhancement

## 1 Closing by Reconstruction

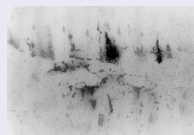
$$F_{Cl} = \Phi(\min_{i=1,\dots,18}\{\phi_{B_i}(F_0)\})$$

## 2 Sum of top-hats

$$F_{th} = \sum_{i=0}^{17} \tau_{B_i}(F_{Cl}) = \sum_{i=0}^{17} (F_{Cl} - \gamma_{B_i}(F))$$

Wrong formula (white objects)!

### Enhancement pipeline



# Crack enhancement

## 1 Closing by Reconstruction

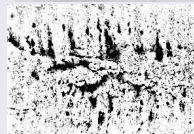
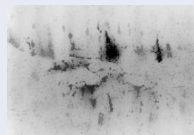
$$F_{Cl} = \Phi(\min_{i=1, \dots, 18} \{\phi_{B_i}(F_0)\})$$

## 2 Sum of top-hats

$$F_{th} = \left( \sum_{i=0}^{17} (\phi_{B_i}(F) - F_{Cl}) \right)^{-1}$$

Very noisy results, omitted.

### Enhancement pipeline



# Crack enhancement

## 1 Closing by Reconstruction

$$F_{Cl} = \Phi(\min_{i=1, \dots, 18} \{\phi_{B_i}(F_0)\})$$

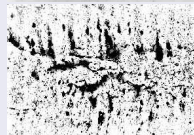
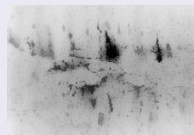
## 2 Sum of top-hats

$$F_{th} = \left( \sum_{i=0}^{17} (\phi_{B_i}(F) - F_{Cl}) \right)^{-1}$$

Very noisy results, omitted.

## 3 Laplacian of Gaussian $F_{lap} = LoG_2^{12}(F_{Cl})$

### Enhancement pipeline



# Crack detection and segmentation

- Final segmentation of cracks

## Segmentation pipeline

# Crack detection and segmentation

- Final segmentation of cracks
- Alternating MM filters

## Segmentation pipeline



# Crack detection and segmentation

- Final segmentation of cracks
  - Alternating MM filters
- 1** Closing by Reconstruction
- $$F_1 = \Phi(\min_{i=1,\dots,18}\{\phi_{B_i}(F_{lap})\})$$

## Segmentation pipeline



# Crack detection and segmentation

- Final segmentation of cracks
  - Alternating MM filters
- 1** Closing by Reconstruction
- $$F_1 = \Phi(\min_{i=1, \dots, 18} \{\phi_{B_i}(F_{lap})\})$$

## Segmentation pipeline



# Crack detection and segmentation

- Final segmentation of cracks
  - Alternating MM filters
- 1 Closing by Reconstruction  

$$F_1 = \Phi(\min_{i=1, \dots, 18} \{\phi_{B_i}(F_{lap})\})$$
  - 2 Opening by Reconstruction  

$$F_2 = \Gamma(\max_{i=1, \dots, 18} \{\gamma_{B_i}(F_1)\})$$

## Segmentation pipeline





# Crack detection and segmentation

- Final segmentation of cracks
  - Alternating MM filters
- 1** Closing by Reconstruction  

$$F_1 = \Phi \left( \min_{i=1, \dots, 18} \{ \phi_{B_i} (F_{lap}) \} \right)$$
  - 2** Opening by Reconstruction  

$$F_2 = \Gamma \left( \max_{i=1, \dots, 18} \{ \gamma_{B_i} (F_1) \} \right)$$
  - 3** Large closing with double scale  

$$F_{final} = \left( \min_{i=1, \dots, 18} \{ \phi_{B_i}^2 (F_2) \} \right)$$

## Segmentation pipeline



1 Introduction

2 Morphology

3 Linear filters

4 Detection

**5 Evaluation**

- Evaluation results from the paper
- Experiments
- Evaluation of the paper

6 Summary

## Criteria for parameter selection

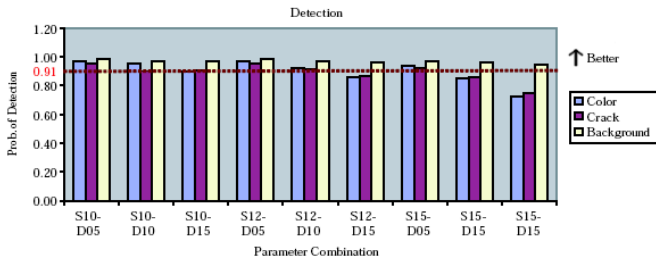
- Parameters:  $S$  length of SE in pixels,  $D$  degree of rotations

## Criteria for parameter selection

- Parameters:  $S$  length of SE in pixels,  $D$  degree of rotations
- Goal: false positive rate below 7%, false negative rate below 2%

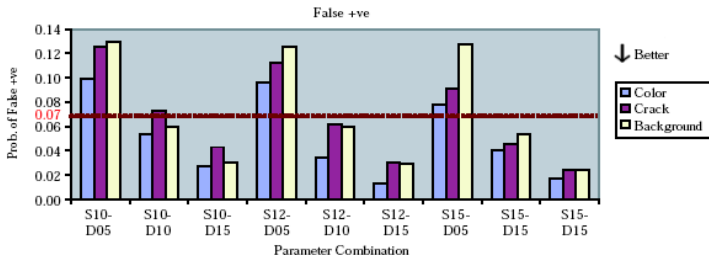
# Criteria for parameter selection

- Parameters:  $S$  length of SE in pixels,  $D$  degree of rotations
- Goal: false positive rate below 7%, false negative rate below 2%
- Probability of detection



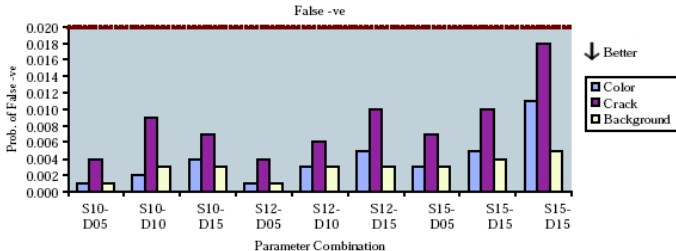
## Criteria for parameter selection

- Parameters:  $S$  length of SE in pixels,  $D$  degree of rotations
- Goal: false positive rate below 7%, false negative rate below 2%
- Probability of false positive (crack detected where is none)



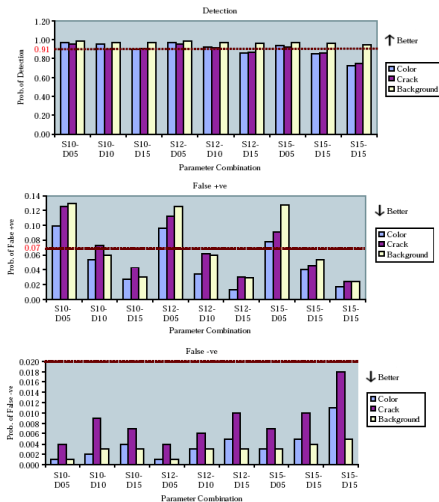
## Criteria for parameter selection

- Parameters:  $S$  length of SE in pixels,  $D$  degree of rotations
- Goal: false positive rate below 7%, false negative rate below 2%
- Probability of false negative (crack not detected)



# Criteria for parameter selection

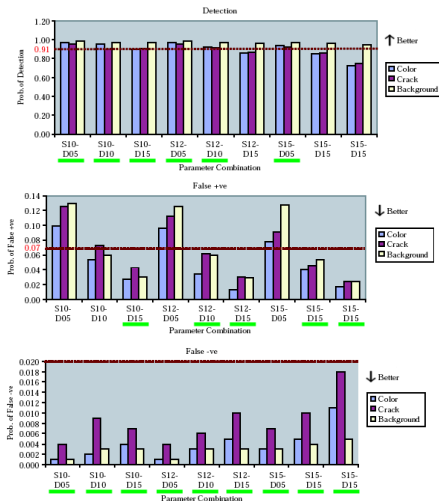
- Probability of detection
- Probability of false positive
- Probability of false negative





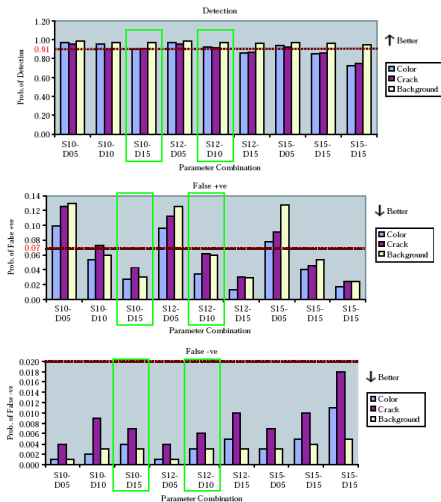
# Criteria for parameter selection

- Probability of detection
- Probability of false positive
- Probability of false negative



# Criteria for parameter selection

- Probability of detection
- Probability of false positive
- Probability of false negative
- Best parameters in paper:  
SE length  $S = 12$  pixel  
and a degree of rotations  
 $D = \text{every } 10^\circ$



# Criteria for comparison to different approaches

- Comparison based on individual evaluation of approaches

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- Ground truth by manually segmenting test images (reference)
- Completeness  $\approx \frac{\# \text{ matched crack pixels of ref.}}{\# \text{ crack pixels of reference}}$  (optimal: 1)
- Correctness  $\approx \frac{\# \text{ matched crack pixels of extraction}}{\# \text{ crack pixels of extraction}}$  (optimal: 1)

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- Comparison based on individual evaluation of approaches
- Ground truth by manually segmenting test images (reference)
- Completeness  $\approx \frac{\# \text{ matched crack pixels of ref.}}{\# \text{ crack pixels of reference}}$  (optimal: 1)
- Correctness  $\approx \frac{\# \text{ matched crack pixels of extraction}}{\# \text{ crack pixels of extraction}}$  (optimal: 1)
- Redundancy
 
$$\approx \frac{\# \text{ matched crack pixels of extr.} - \# \text{ matched pixels of ref.}}{\# \text{ crack pixels of extraction}}$$
 (optimal: 0)

# Criteria for comparison to different approaches

- Comparison based on individual evaluation of approaches
- Ground truth by manually segmenting test images (reference)
- Completeness  $\approx \frac{\# \text{ matched crack pixels of ref.}}{\# \text{ crack pixels of reference}}$  (optimal: 1)
- Correctness  $\approx \frac{\# \text{ matched crack pixels of extraction}}{\# \text{ crack pixels of extraction}}$  (optimal: 1)
- Redundancy  
 $\approx \frac{\# \text{ matched crack pixels of extr.} - \# \text{ matched pixels of ref.}}{\# \text{ crack pixels of extraction}}$  (optimal: 0)
- Quality  $\approx \frac{\text{compl} \cdot \text{corr}}{\text{compl} - \text{compl} \cdot \text{corr} + \text{corr}}$  (optimal: 1)



## Criteria for comparison to different approaches

- Comparison based on individual evaluation of approaches
- Ground truth by manually segmenting test images (reference)
- Completeness  $\approx \frac{\# \text{ matched crack pixels of ref.}}{\# \text{ crack pixels of reference}}$  (optimal: 1)
- Correctness  $\approx \frac{\# \text{ matched crack pixels of extraction}}{\# \text{ crack pixels of extraction}}$  (optimal: 1)
- Redundancy  
 $\approx \frac{\# \text{ matched crack pixels of extr.} - \# \text{ matched pixels of ref.}}{\# \text{ crack pixels of extraction}}$  (optimal: 0)
- Quality  $\approx \frac{\text{compl} \cdot \text{corr}}{\text{compl} - \text{compl} \cdot \text{corr} + \text{corr}}$  (optimal: 1)
- Parameters for other approaches not mentioned in paper

# Different approaches

## Otsu's thresholding

- Apply thresholds to detect cracks
- Separates a number of intensity classes
- Uses statistical methods to minimize variance in a class and at the same time maximize the variance between the classes

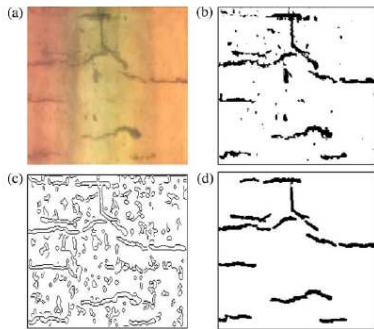


Fig. 13. Edge detection algorithms on crack pattern image: (a) original image, (b) Otsu's thresholding (c) Canny's edge detector, and (d) proposed approach.

# Different approaches

## Otsu's thresholding

- Apply thresholds to detect cracks
- Separates a number of intensity classes
- Uses statistical methods to minimize variance in a class and at the same time maximize the variance between the classes

## Canny's edge detection

- Detect edges in the image between crack and background
- Uses linear filters (Gaussian and Sobel)
- Apply Gaussian, then apply a series of gradient filters to detect edges in different directions

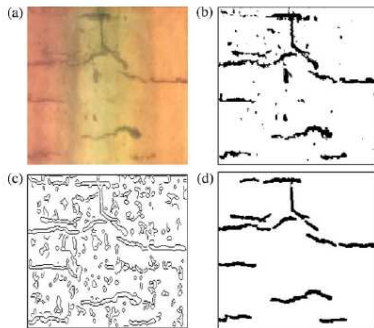


Fig. 13. Edge detection algorithms on crack pattern image: (a) original image, (b) Otsu's thresholding (c) Canny's edge detector, and (d) proposed approach.

# Comparison to different approaches

- Otsu's thresholding
- Canny's edge detector
- No information about parameters in paper

# Comparison to different approaches

- Otsu's thresholding
- Canny's edge detector
- No information about parameters in paper

Paper approach

Class	Cracks	Background	Color
Completeness	0.95	0.88	0.90
Correctness	0.98	0.94	0.91
Quality	0.93	0.83	0.83
Redundancy	0.00	-0.01	0.00

# Comparison to different approaches

- Otsu's thresholding
- Canny's edge detector
- No information about parameters in paper

Paper approach

Class	Cracks	Background	Color
Completeness	0.95	0.88	0.90
Correctness	0.98	0.94	0.91
Quality	0.93	0.83	0.83
Redundancy	0.00	-0.01	0.00

Otsu's thresholding

Class	Cracks	Background	Color
Completeness	0.98	0.61	0.62
Correctness	0.37	0.45	0.08
Quality	0.37	0.35	0.08
Redundancy	0.22	0.23	0.24

# Comparison to different approaches

- Otsu's thresholding
- Canny's edge detector
- No information about parameters in paper

## Paper approach

Class	Cracks	Background	Color
Completeness	0.95	0.88	0.90
Correctness	0.98	0.94	0.91
Quality	0.93	0.83	0.83
Redundancy	0.00	-0.01	0.00

## Otsu's thresholding

Class	Cracks	Background	Color
Completeness	0.98	0.61	0.62
Correctness	0.37	0.45	0.08
Quality	0.37	0.35	0.08
Redundancy	0.22	0.23	0.24

## Canny's edge detector

Class	Cracks	Background	Color
Completeness	0.92	0.61	0.62
Correctness	0.20	0.44	0.07
Quality	0.20	0.34	0.07
Redundancy	0.15	0.17	0.14

# Comparison to different approaches

- Otsu's thresholding
- Canny's edge detector
- No information about parameters in paper
- Very good evaluation results for proposed method in paper (not verified)

Paper approach

Class	Cracks	Background	Color
Completeness	0.95	0.88	0.90
Correctness	0.98	0.94	0.91
Quality	0.93	0.83	0.83
Redundancy	0.00	-0.01	0.00

Otsu's thresholding

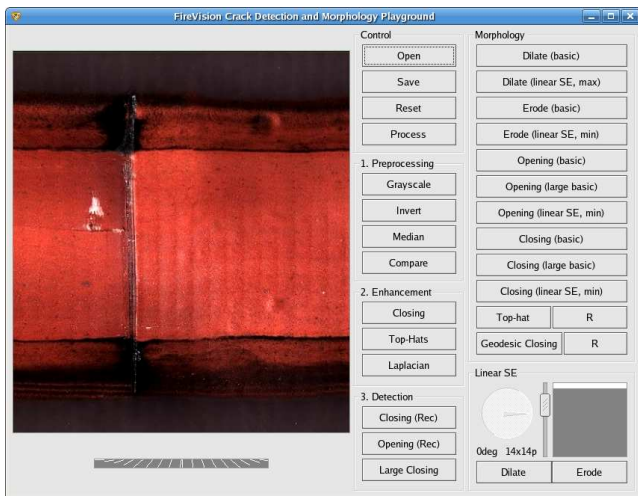
Class	Cracks	Background	Color
Completeness	0.98	0.61	0.62
Correctness	0.37	0.45	0.08
Quality	0.37	0.35	0.08
Redundancy	0.22	0.23	0.24

Canny's edge detector

Class	Cracks	Background	Color
Completeness	0.92	0.61	0.62
Correctness	0.20	0.44	0.07
Quality	0.20	0.34	0.07
Redundancy	0.15	0.17	0.14

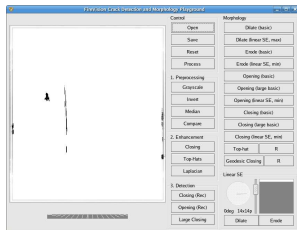
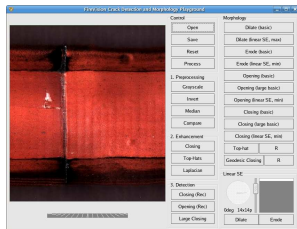


# FireVision Crack Detection and Morphology Sandbox



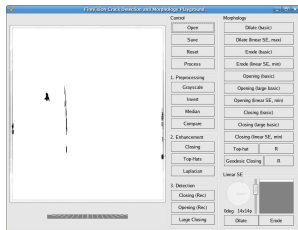
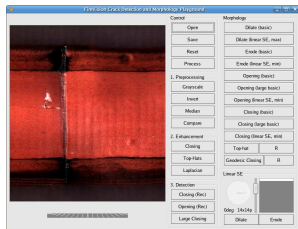
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- Implemented in FireVision RoboCup vision framework from AllemaniACs RoboCup team



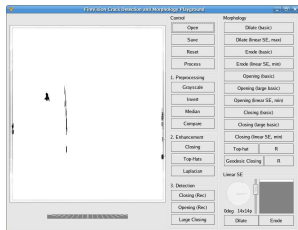
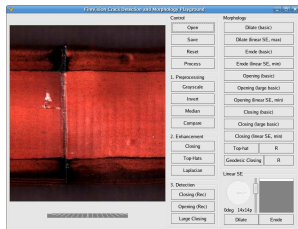
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- Implemented in FireVision RoboCup vision framework from AllemaniACs RoboCup team
- Parameters adapted to sample images supplied by Institut für medizinische Informatik
- Revealed several pieces of missing information and errors



# Zana and Klein

Frederic Zana and Jean-Claude Klein: Segmentation of vessel-like patterns using mathematical morphology and curvature evaluation. *IEEE Transactions on Image Processing*, 10(7):1010-1019, July 2001.

- Basically the template of the discussed paper

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- Basically the template of the discussed paper
- Proposed algorithm the same, just extracts brightest part of image
- More evaluation in discussed paper
- Discussed paper *very* similar



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1 Introduction

2 Morphology

3 Linear filters

4 Detection

5 Evaluation

**6 Summary**

- Conclusion
- End of Talk



# Paper Resume

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- Presented approach uses mathematical morphology and curvature evaluation and makes use of a priori knowledge about crack structures
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- Paper is derived from another paper and *very similar*

# Questions?

Information compiled at  
<http://www.niemueller.de/uni/crackdet/>